RESEARCH Open Access

CrossMark

Development of multi-pitch tool path in computer-controlled optical surfacing processes

Jing Hou^{1,2}, Defeng Liao^{1,2*} and Hongxiang Wang¹

Abstract

Background: Tool path in computer-controlled optical surfacing (CCOS) processes has a great effect on middle spatial frequency error in terms of residual ripples. Raster tool path of uniform path pitch is one of the mostly adopted paths, in which smaller path pitch is always desired for restraining residual ripple errors. However, too dense paths cause excessive material removal in lower removal regions deteriorating the form convergence.

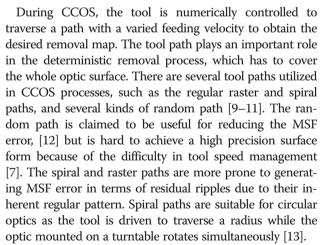
Methods: With this in view, we propose a novel tool path planning method named multi-pitch path. With the path, the material removal map is divided into several regions with varied path pitches according to the desired removal depth in each region. The path pitch is designed larger at low removal regions while smaller at high removal regions, and the feeding velocity of the tool is maintained at high level when scanning the whole surface.

Results and conclusions: Experiments were conducted to demonstrate this novel tool path planning method, and the results indicate that it can successfully restrain the residual ripples, and meanwhile guarantee favorable convergent rate of form error.

Keywords: Multi-pitch tool path, Middle spatial frequency error, Residual ripple, Removal regions

Background

Large optics has been widely used in interferometers, telescopes, high-power lasers and other optical systems. In these systems, the optics are required of stringent specifications of low, middle and high spatial frequency errors [1, 2]. Various CCOS processes have been developed which can provide good solutions for the fabrication of these optics because of their high convergence rates of low frequency error (i.e. surface form) [3-5]. Nowadays, more and more attentions have been paid to the middle spatial frequency (MSF) error, which is crucial for image performance and beam quality [6]. MSF error is primarily introduced during the CCOS processes, and it is hard to restrain. It is reported that MSF error is mainly affected by the initial surface error distribution (spatial and frequency domain), the removal function characters (profile, removal efficiency and stability) and the adopted paths [7, 8].



Raster path is usually adopted for the fabrication of square-shaped optics. During polishing with raster path, the tool feeds along a straight line and then translates to another parallel line. This process is repeated to cover the whole surface. The pitch between adjacent path lines is commonly set identical (i.e. uniform pitch) on the whole surface, and the feeding velocity along each path



^{*} Correspondence: defeng_liao@163.com

¹School of Mechatronics Engineering, Harbin Institute of Technology, Harbin 150001, China

²Research Center of Laser Fusion, China Academy of Engineering Physics, Mianyang 621900, China

is instantaneously controlled based on the local removal [14]. It is obvious that for a uniform removal map of a certain removal amount, the smaller the path pitch, the larger the feeding velocity. However, if the desired feeding velocity is larger than the largest one allowed by the machine, the actual feeding velocity has to be changed to the largest one, which will introduce extra dwell time leading to material over-removal. As the tool feeds fast at lower region while slowly at higher region with the uniform pitch path, the smallest removal region (lowest region) will commonly bring with such over-removal. Since, the decreased pitch is propitious to restraint of MSF errors [15]. On the other hand, the decreased pitch will greatly increase over-removal especially in the lowest region deteriorating the form correction precision. Hence, it is needed to develop an optimized tool path planning method which can solve this problem.

A novel tool path planning method named multi-pitch path, is developed in this paper. With this method, the material removal map is divided into several regions with varied path pitches according to the desired removal depth in each region. The path pitch is designed larger at low removal regions, so as to bring much less over-removal; while smaller at high removal regions, so as to decrease MSF error in terms of the residual ripples. The path has obvious advantage in restraint of residual ripples, and meanwhile can guarantee convergent rate of form errors. In the following section II, the correlation between the ripple and MSF error is analyzed to verify the rationality of characterizing the MSF error by ripples. In section III, the factors impacting ripple errors, including the removal amount and path pitch are discussed. In section IV, the multi-pitch path and polishing procedure with the path are detailed and the experimental validation is conducted.

Method

Verification of characterizing MSF errors with the residual ripple

Spatial frequency of surface errors is divided into several separate bands in the field of high power lasers [2]: surface figure (>33 mm), MSF error (0.12 \sim 33 mm) and

surface roughness (0.01 \sim 0.12 mm). There are two types of specification for MSF error; one is RMS value after band pass filtering, and the other is a not-to-exceed line for the power spectral density (PSD) as a function of spatial frequency [16]. In the following, we select RMS after band pass filtering over 0.12 \sim 33 mm range for evaluation of the MSF error.

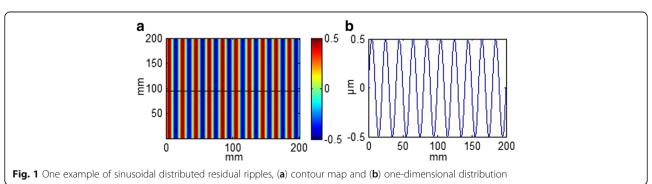
MSF errors induced by CCOS processes are commonly in form of residual ripples. Thus, in order to quantitatively specify the correlation between residual ripple error and MSF error, we formulated a series of sinusoidal surface forms with variable spatial frequency and magnitude (see Fig. 1). The surface forms are sinusoidal distributed in x direction, while are uniformly distributed in y direction. Surface forms of this shape are fairly similar to the local regions of surface forms practically corrected by CCOS processes, which are nearly sinusoidallydistributed in the scanning direction while nearly uniformly-distributed in the feeding direction. Herein, the MSF error, in terms of the RMS value in the midspatial frequency band (0.0303 ~ 8.33 mm⁻¹), is calculated for all the surface forms as shown in Fig. 2. It is revealed that the spatial frequency has little effect on the RMS value, while there has a good linear relationship between the spatial magnitude and the RMS value. Thus, we should focus on the residual ripple magnitude rather than the frequency while restraining MSF errors.

Influencing factors of residual ripple errors

As revealed above that residual ripple error can be characterized by the ripple amplitude, i.e. the peak-to-valley value of the ripple (PVe). We introduce a normalized PV value of residual ripple (PVn), which is derived from PVe divided by the average removal depth (r). PVn represents the residual error PVe while achieving unit removal (see Eq.1).

$$PV_{n} = PV_{e}/r \tag{1}$$

Primary factors impacting the residual ripple errors include the scanning pitch (i.e., path pitch), removal depth, and tool influence function (TIF) features. Without loss



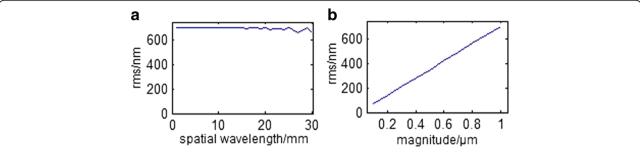
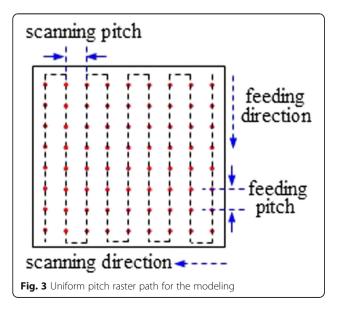


Fig. 2 The relationships between the MSF error and the ripple features. a Rms and ripple frequency and (b) Rms and ripple magnitude (Rms after band pass: 0.12-33 mm)

of generality, we modelled variable scanning pitch resulting in a uniform removal map as well as variable removal map under the same scanning pitch, to reveal the effects of the canning pitch and removal depth on the residual ripple and MSF error. Herein, we consider a Magnetorheological Finishing (MRF) TIF traversing a uniform pitch raster path, under the condition that the feeding direction is set in perpendicular to the fluid flow direction as shown in Figs. 3 and 4. As the TIF traverses a single line path with a constant feeding velocity of ν , the removal is uniformly distributed along the feeding direction, while the removal distribution R_j in the perpendicular direction can be obtained by Eq.2 (see Fig. 5), in which TIF matrix (R, unit in um/s) has s row, k column elements as shown in Eq.3; and the pixel size is p (unit in mm).

$$R_j = p/\nu \cdot \sum_{i=1}^k r_{i,j}, \ j = 1, ..., l.$$
 (2)



$$R = \begin{bmatrix} r_{11} & r_{12} \cdots & r_{1k} \\ r_{11} & r_{12} \cdots & r_{1k} \\ \cdots & \cdots & r_{ij} \cdots \\ r_{s1} & r_{s2} \cdots & r_{sk} \end{bmatrix}$$
(3)

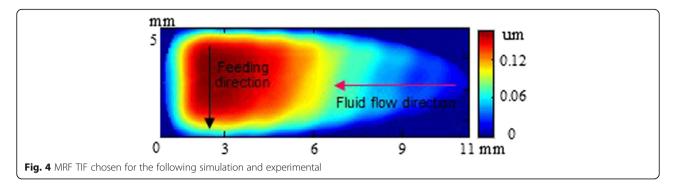
Figure 6 shows the local removal amount distribution in the scanning direction while correcting uniformly-distributed form errors. The blue sections represent the removal amount in independent single path and the red one is the convolved removal amount. It is obvious that the convolved removal amount is periodically distributed, and the spatial wavelength is identical to the scanning pitch. It is confirmed that surface form correction by small-sized TIF inevitably induces residual ripple error.

Figure 7a shows that PVe becomes a linear growth along with the increment of the removal amount. It is suggested that a less removal amount is propitious to restraint of PVe. Figure 7b shows the PVn value as a function of scanning pitch. PVn increases as the scanning pitch is increased. It is noticeable that PVn increases slowly until the scanning pitch reaches ~1.1 mm, and then increases sharply. It is revealed that while correcting the surface form of optics by sub-aperture polishing, it is desired to adopt a smaller tool-path pitch for restraint of residual ripple.

Development of the multi-pitch tool path

Correction of the form error by CCOS processes aims to polish every region to a desired plane of absolute flatness, which is commonly located at the lowest point on the surface as shown in Fig. 8. In fact, a lower plane has to be selected due to the maximum motion speed of the tool. Such a removal map introducing extra removal isn't propitious to restraint of residual ripples as revealed above.

If the desired plane selected at the lowest point, the desired removal amount at the point would be zero. As



the tool traverses across the point, it inevitably removes material deteriorating figure convergence, thus the tool are commonly driven with a most velocity allowable for the machine. Furthermore, the path pitch within lowest regions should be as large as possible so as to introduce less over-removal, but in uniform pitch tool path, a large pitch would deteriorate the residual ripple errors. Therefore, we develop a multi-pitch tool path which has a large pitch in less removal regions reducing over-removal and small pitch in more removal regions so as to decrease the residual ripples while guaranteeing the figure convergence.

The polishing procedure with the multi-pitch tool path is showed in Fig. 9. First, we should generate the removal map according to the actual surface figure and the desired surface figure. Then, the removal map is divided into several subregions based on the removal variance. After that we calculate the scanning path pitch and generate the path for each subregion. The spacing between adjacent dwell points along each path line, i.e. the feeding pitch, is also determined. The feeding pitch can be adopted within a wide range, yet value of the scanning pitch is recommended. After determination of the scanning and feeding pitches, we then acquire the dwell points on the whole surface. The polishing time at each dwell point (i.e. the dwell map) can be solved with various algorithms such as discrete convolution model, the linear equation model and so forth [17]. Finally, the CNC code can be generated according to the dwell point on the path and the dwell time map.

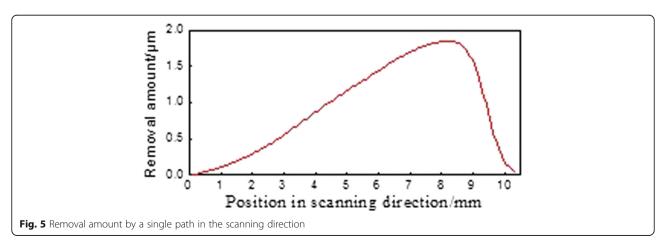
Determination of the path pitch in each subregion

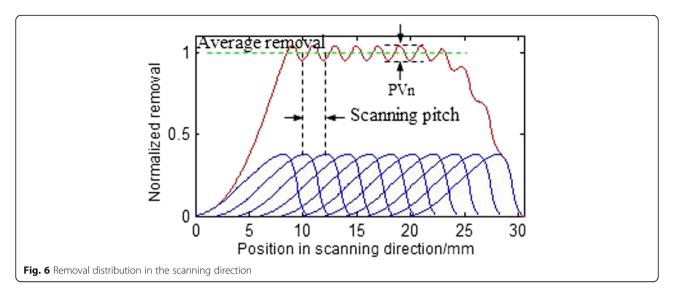
While generating multi-pitch tool path, we first divide the optic surface into several subregions according to the removal map. The whole material removal scope within the maximum and minimum removals is divided into several ranges, and then each removal range determines the corresponding subregions. The number of the removal ranges or subregions depends on the whole removal scope; the larger the removal, the more the ranges or subregions. Generally, $3 \sim 6$ removal ranges or subregions are appropriate for most cases. Assuming a removal map has a maximum removal of r and a minimum removal of r0, it is divided into r1 subregions and the removal variance in each subregion has the same value r2, then the removal in each subregion can be derived by Eqs.4–5.

$$(k-1)\cdot\Delta r \le r_k < k\cdot\Delta r, \quad k = 1, ..., m. \tag{4}$$

$$\Delta r = r/m \tag{5}$$

While determining the path pitch in a subregion, a dwell point P which has a removal of h and covers a square area in the subregion is considered, as shown in Fig. 10. The removal is almost uniformly distributed in the tiny square area, and then the correlation among the





removal depth (r), path pitch (d) and feeding velocity (ν) can be obtained by Eq.6. It is revealed that a certain d can be calculated for a given s, r and $\nu_{\rm max}$, as shown in Eq.7.

$$s = r \cdot d \cdot v \tag{6}$$

$$d = s/(r \cdot v_{\text{max}}) \tag{7}$$

In Eqs.6-7 h represents the feeding pitch, $v_{\rm max}$ the largest feeding velocity allowed by the machine, and s is the volume removal rate of the TIF, which can be derived by Eq.8:

$$s = p^2 \cdot \sum_{i=1}^{l} \sum_{i=1}^{k} R_{i,j}$$
 (8)

Where p (unit in mm) is the pixel size of the TIF, and Ri,j (unit in um) is the TIF removal rate.

As revealed in the previous section, minimum path pitches are desired for restraint of residual ripple errors. Eq.7 indicates that the feeding velocity is inversely proportional to the pitch; thus, we can adopt a maximum feeding velocity allowed by the machine so as to decrease the pitch.

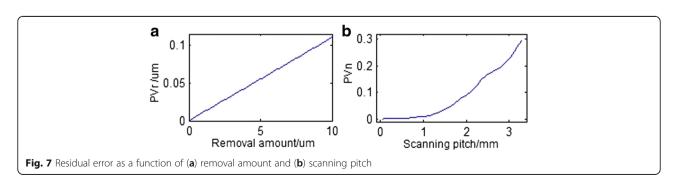
However, increasing feeding velocity has a significant impact on the stability of TIF. A too large feeding velocity will result in alteration of TIF, and hence deteriorate efficiency of figure correction as well as MSF errors. Further, the machine imposes restrictions on the moving velocity and acceleration of every movable component. Hence, there is a favorable maximum velocity allowed for each polishing machine. Herein, the largest feeding velocity ($\nu_{\rm max}$) allowed by the machine can be adopted in practice so as to reduce the pitch and hence the PVe.

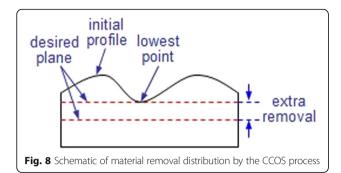
As each subregion is determined within a material removal range, we adopt the minimum removal depth in each region for calculation of the corresponding path pitch (see Eq.9), which will prevent the feeding velocity exceeding the specified maximum value. Then, the pitch in each region can be obtained by Eq.10.

$$r_1 = 0.5 \cdot dr, r_k = (k-1) \cdot dr, \quad k = 2, ..., n.$$
 (9)

$$d_k = s/(r_k \cdot v_{\text{max}}) \tag{10}$$

In CCOS processes, the scanning path pitch should be restricted within a range in practice. The minimum value of the pitch is determined by the positioning & moving precision of the polishing machine. The maximum one is

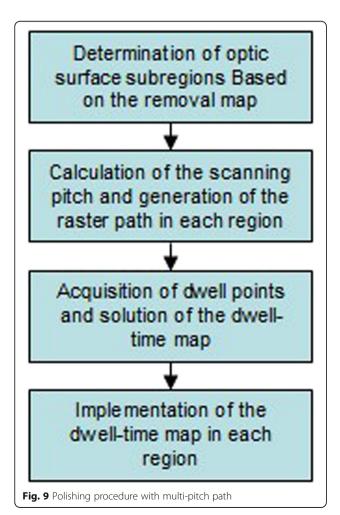


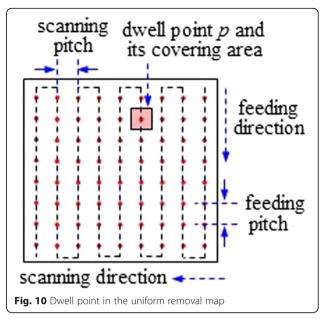


primarily dependent on the TIF size (i.e. <1/6 size). Further, a too large path pitch isn't propitious to correcting the form error and restraining the ripple error.

Solution and implementation of dwell time map

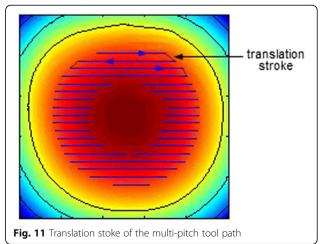
Dwell time map in terms of the polishing time at each dwell point provides the time that the tool dwells on the corresponding position to obtain desired removal. In the multi-pitch tool path, the dwell points are allocated at each path line with a feeding pitch. The

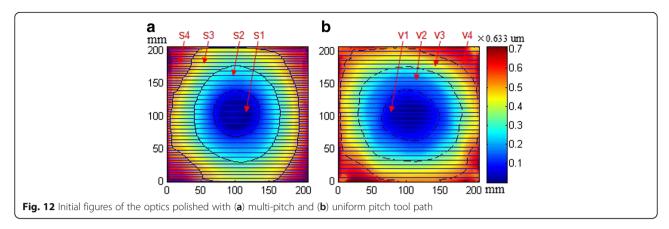




feeding pitch can be specified according to the scanning pitch. Then, the dwell time map is solved by any developed algorithms, such as the discrete convolution method, linear equation method and so forth. The local feeding velocity (ν_f) can be derived from the pitch and the local removal (r_f) at the corresponding point, as revealed in Eqs.11–12. In the multi-pitch tool path, the removal variance in each region is greatly decreased compared to the conventional tool path with a constant pitch on the whole optic surface. As the tool scans the path lines in any subregion, the path pitch is decreased as much as possible in every region, which is prone to improving the implementation precision of the dwell-time.

$$s \cdot t = r_f \cdot d \cdot v_f \cdot t \tag{11}$$





$$v_f = s/(d \cdot r_f) \tag{12}$$

During generation of multi-pitch tool path, the optic surface is divided into several regions. In each region, the tool scans a raster path with a featured constant pitch. The pitch is dependent on the removal in the region, and the larger the removal, the smaller the pitch. During implementation of the dwell time map, the tool will traverse all the paths that generated covering the whole surface. Herein, we suggest that each region be scanned individually. In each region, adjacent path lines can be interconnected at the ends during implementation of the dwelltime map. As the tool traverses a path line and reaches the end, it translates to the nearby end of the next line and traverses this line (see Fig. 11). The translation stroke from one line to another maybe introduces extra dwell time, which will cause undesired removal and deteriorate the convergence rate of the surface form. If the tool lifts up after completing the last feeding segments in each path line, it will inevitably introduce extra removal during the lifting process. It is suggested that the tool lifts up while traversing the last feeding segment within a period longer than the determined dwell time. At this condition, the increased actual dwell time will compensate the decreased removal function achieving approximately the desired removal. Similarly, the tool descends while traversing the first feeding segment of the next path line. After the tool has covered one subregion, it also lifts off the optic and translates above to the first dwell point of another subregion. Then it descends to accomplish the subsequent dwell time. The lifting of the tool during the translation process wouldn't bring with extra removal.

Results and discussion

Herein, we utilize the multi-pitch tool path and regular uniform pitch tool path for figure correction with MRF process. The two paths are compared through simulation and experiments.

MRF process is a typical CCOS process characterized by the stable TIF and deterministic figuring procedure. The MRF machine has x, y, z axes for translation motions, C axis for rotation motion and A axis for swing motion. The maximum translating velocity of the x, y, z axes allow for 50 mm/s. The diameter of the wheel is 300 mm. The spotting and figuring processes are conducted under the condition: wheel speed 200 rpm, MR fluid ribbon height 1.6 mm and the penetration depth of the optic into the ribbon 0.4 mm. The magnetic field strength applied to the MR fluid ribbon is also stably controlled. The TIF obtained by spotting process is showed in Fig. 4.

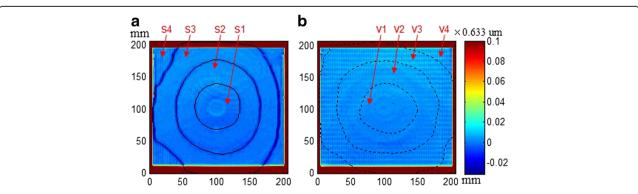
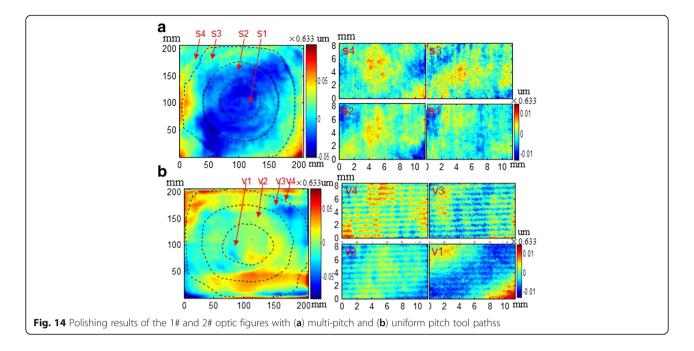


Fig. 13 Simulation results of the 1# and 2# optic figures with (a) multi-pitch and (b) uniform pitch tool paths. PVe of S1 \sim S4 are all smaller than 0.01 λ , while PVe of V1, V2, V3, V4 are approximately 0.008, 0.02, 0.04, 0.06 λ



We used two 200 mm \times 200 mm sized optics (1#,2#). The optics are previously ground and polished with continuous polishing process. They both have a favorable initial MSF error specification because the continuous polishing has distinct advantage in restraint of MSF errors. Figures of the both are similarly distributed with a PV value of approximately 0.443um, as shown in Fig. 12. In the following, we employed the TIF to correct the optic figures respectively.

The practical feeding velocity is set to 50 mm/s for determining the pitches. We then calculate the desired pitch for each removal depth by Eq.7. Herein, 1# optic is polished with multi-pitch tool path, while 2# optic with uniform pitch tool path for

comparison. The removal map of 1# optic is divided into 4 regions, and the removal depths in the regions are as follows: 1) 0 \sim 0.0633um, 0.0633 \sim 0.190um, 0.190 \sim 0.316um, 0.315 \sim 0.443um, then the pitches in the regions can be obtained: 0.8, 0.395, 0.132, 0.099 mm. The pitch of 2# optic is set at 0.8 mm on the whole surface.

The dwell points are generated with a feeding pitch of 0.3 mm along every path, and the dwell time map is solved by common discrete convolution algorithm. Then the CNC code for controlling the kinematics of the MRF machine is generated based on the dwell point and dwell time. The simulation and experimental results are shown in Figs. 13, 14 and 15.

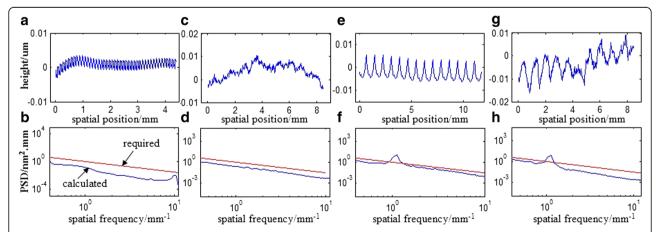


Fig. 15 Residual profiles and PSD errors of the simulation and polishing results, the sampling area is part of the subregions. **a** Residual profile of S4 simulation, **b** PSD error of S4 simulation, **c** residual profile of S4 polishing results, **d** PSD error of S4 polishing results, **e** residual profile of V4 simulation, **f** PSD error of V4 simulation, **g** residual profile of V4 polishing results, **h** PSD error of V4 polishing results

The both optics have a surface form of approximately 0.095um PV after polishing with multi-pitch and uniform pitch tool paths respectively in simulation and experiments. In the uniform pitch path, the residual ripples are fairly large and non-uniformly distributed depending on the local removal. The regions with more removal have larger residual ripples. In contrast, the multi-pitch polished optic exhibits superiority in restraining residual ripple. As the more removal regions with a much smaller pitch path, the residual ripples are restrained. It is noticeable that the optic polished with multi-pitch path has slight depression at the edge between adjacent regions due to that the tool translation stroke from one path line to another introduces extra removal. Although, the depression is so small that it has little effect on the figure error.

Conclusions

A multi-pitch tool path was developed for CCOS processes. With this tool path, the removal map is divided into several subregions, and the pitch in each subregion is set individually. In small removal subregions, the pitch is larger introducing less extra removal so that guarantee the convergence of the figure correction, while the large removal subregions the pitch is smaller so as to decrease the residual ripples. The multi-pitch tool path has been verified that it is beneficial to restraining the ripples while maintaining the convergence of the figure correction.

Abbreviations

CCOS: Computer-controlled optical surfacing; MRF: Magnetorheological Finishing; MSF: Middle spatial frequency; PSD: Power spectral density; PVe: Peak-to-valley value of the ripple; PVn: Normalized PV value of residual ripple; TIF: Tool influence function

Acknowledgements

Not applicable.

Funding

This work was supported by Science Challenge Project of China, No. JCKY2016212A506–0501.

Availability of data and materials

Data will be shared after publication.

Authors' contributions

DL and JH developed the multi-pitch tool path; HW assisted conducting the experiments. All authors read and approved the final manuscript.

Ethics approval and consent to participate

Not applicable.

Consent for publication

Not applicable.

Competing interests

The authors declare that they have no competing interests.

Publisher's Note

Springer Nature remains neutral with regard to jurisdictional claims in published maps and institutional affiliations.

Received: 14 June 2017 Accepted: 24 August 2017 Published online: 09 September 2017

References

- Betti, R., Hurricane, O.A.: Inertial-confinement fusion with lasers [J]. Nat. Phys. 12(5), 435–448 (2016)
- Pohl, M., Börret, R.: Simulation of mid-spatials from the grinding process [J].
 J. Eur. Opt. Society-Rapid Publ. 11, (2016)
- Almeida, R., Börret, R., Rimkus, W., et al.: Polishing material removal correlation on PMMA–FEM simulation [J]. J. Eur. Opt. Society-Rapid Publ. 11, (2016)
- Wang, C.J., Cheung, C.F., Ho, L.T., et al.: A novel multi-jet polishing process and tool for high-efficiency polishing [J]. Int. J. Mach. Tools Manuf. 115, 60–73 (2017)
- Arnold, T., Boehm, G., Paetzelt, H.: New freeform manufacturing chain based on atmospheric plasma jet machining [J]. J. Eur. Opt. Society-Rapid Publ. 11. (2016)
- Tamkin, J.M., Milster, T.D.: Effects of structured mid-spatial frequency surface errors on image performance [J]. Appl. Opt. 49(33), 6522–6536 (2010)
- Hu, H., Dai, Y., Peng, X.: Restraint of tool path ripple based on surface error distribution and process parameters in deterministic finishing [J]. Opt. Express. 18(22), 22973–22981 (2010)
- Wang, C., Yang, W., Ye, S., et al.: Restraint of tool path ripple based on the optimization of tool step size for sub-aperture deterministic polishing [J]. Int. J. Adv. Manuf. Technol. 75(9–12), 1431–1438 (2014)
- Dai, Y.F., Shi, F., Peng, X.Q., et al.: Restraint of mid-spatial frequency error in magneto-rheological finishing (MRF) process by maximum entropy method [J]. Sci. China Ser. E: Technol. Sci. 52(10), 3092–3097 (2009)
- Wang, C., Wang, Z., Xu, Q.: Unicursal random maze tool path for computercontrolled optical surfacing. Appl. Opt. 54(34), 10128–10136 (2015 Dec 1)
- 11. Yu, G., Li, H., Walker, D.: Removal of mid spatial-frequency features in mirror segments [J]. J. Eur. Opt. Society-Rapid Publ. 6, (2011)
- Dunn, C.R., Walker, D.D.: Pseudo-random tool paths for CNC sub-aperture polishing and other applications [J]. Opt. Express. 16(23), 18942–18949 (2008)
- Walker, D.D., Yu, G., Bibby, M., et al.: Robotic automation in computer controlled polishing [J]. J. Eur. Opt. Society-Rapid Publ. 11, (2016)
- Zhang, X., Yu, J., Zhang, Z., et al.: Analysis of residual fabrication errors for computer controlled polishing aspherical mirrors [J]. Opt. Eng. 36(12), 3386–3391 (1997)
- Cheng, H.B.: Independent variables for optical surfacing systems [M], p. 76.
 Springer-Verlag, Berlin (2014)
- Spaeth, M.L., Manes, K.R., Widmayer, C.C., et al.: The National Ignition Facility wavefront requirements and optical architecture [Cl. SPIE. 5341, 25–42 (2004)
- Wang, C., Yang, W., Wang, Z., et al.: Dwell-time algorithm for polishing large optics [J]. Appl. Opt. 53(21), 4752–4760 (2014)

Submit your manuscript to a SpringerOpen journal and benefit from:

- ► Convenient online submission
- ► Rigorous peer review
- ► Open access: articles freely available online
- ► High visibility within the field
- ► Retaining the copyright to your article

Submit your next manuscript at ▶ springeropen.com